



Koninklijk Nederlands  
Meteorologisch Instituut  
*Ministerie van Infrastructuur en Milieu*

## Extremes in climate science 31.01.2012

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With material from Albert Klein Tank (KNMI)

- Why extremes?
- Moderate extremes
- “Real” extremes
- Modelling extremes
- Changing extremes
- Research questions



# Climate and the climate system



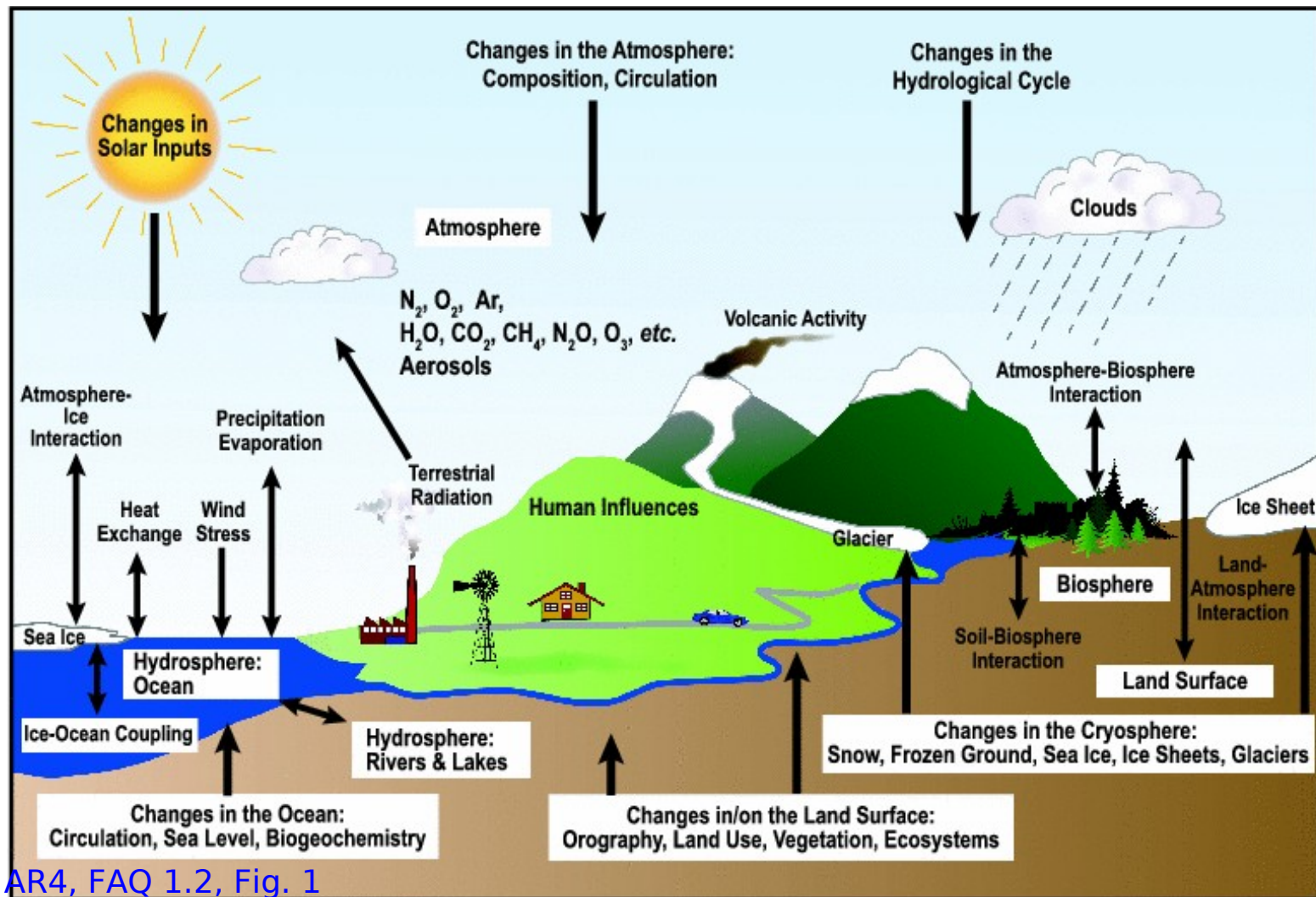
## Climate – what's that?

Climate = statistics of weather

Weather = state of atmosphere at a particular time

“Climate is what you expect, weather is what you get”

# The climate system



AR4, FAQ 1.2, Fig. 1



# Chaotic system

- Multitude of **physical, chemical and biological** processes interacting
  - Length scales from **millimetres to 1000 km**
  - Time scales from **seconds to centuries** (and beyond)
  - **External** (non-deterministic) **influences**: sun, volcanoes, anthropogenic effects (GHG emissions)
- => deterministic forecast limited to ~10 days (**weather**)
- => only statistics beyond (**climate**)



# Climate change

GHG concentrations increase

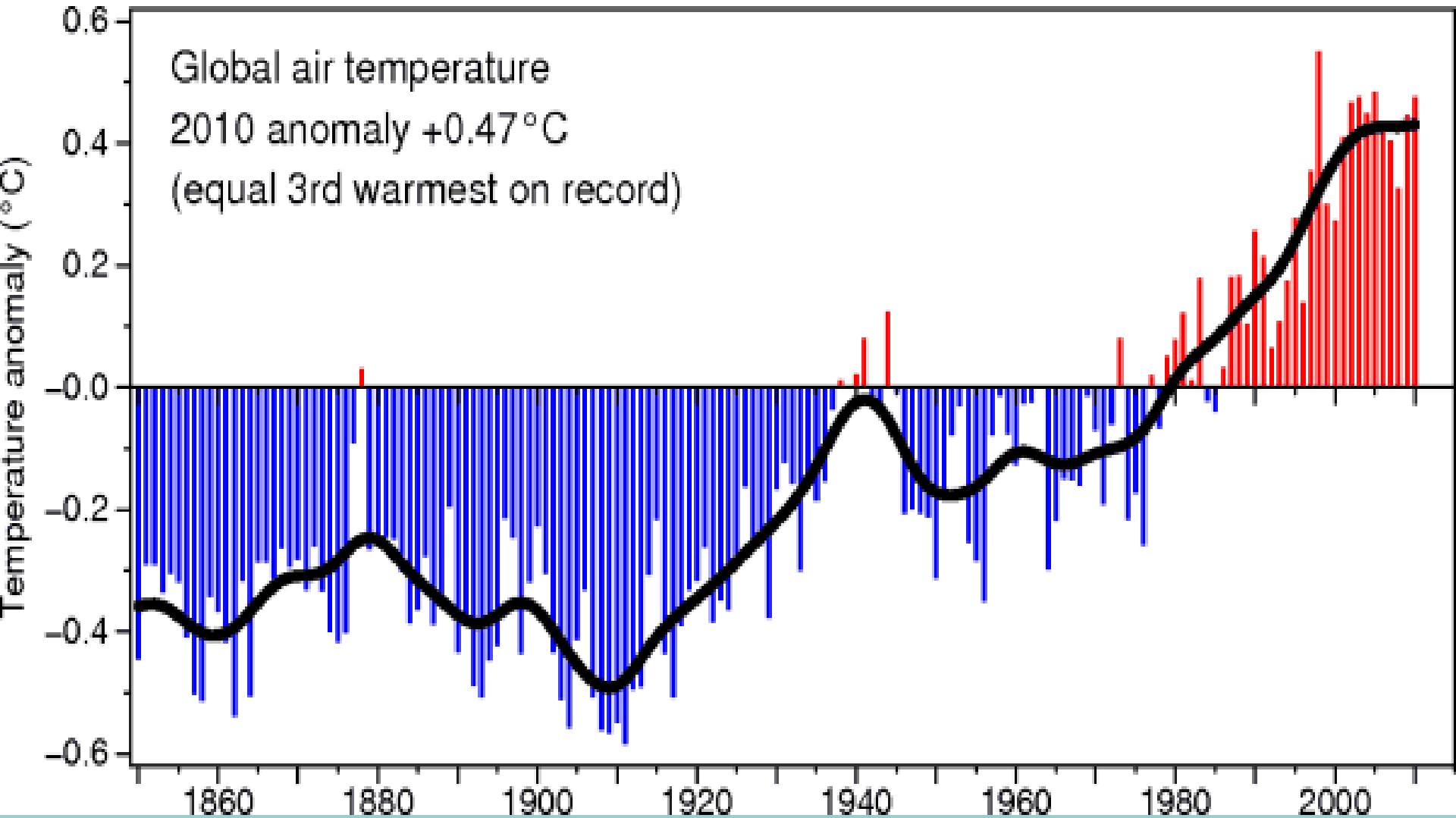
=> Temperature increases

=> other weather elements (wind, precip, clouds) change

Question: **How do their statistical properties (esp. extremes) change?**



# The past 161 years





# Extremes



# Extremes

High impact ([vulnerability](#))

Rare events (tentatively: once per >10 years)

- › May not have occurred in known history -> [Extrapolation](#)
- › Extreme value theory (EVT)

Moderate (soft) extremes (tentatively: once per year; [simple, robust](#))

Climate indices, e.g.

- › TX90p: warm days (= number of days with  $T > 90\%$ -ile)
- › RX5D: monthly maximum of consecutive 5-day precipitation

Wide range of space and time scales:

From very small scale (tornadoes) to large scale (drought)

Change of extremes under [climate change](#)



## Vulnerability

Societies / ecosystems / infrastructures are well-adapted to their mean climate, including “moderate” variability, ...

... but vulnerable to extremes ( $p < 10^{-1}/y$ ) due to exceeded thresholds

Mean climate change is small compared to natural variability, but ...

... thresholds will be exceeded more often

**Question: How often?**



## Analysis of extremes

Rare events:

Requires **long** and **homogeneous** time series

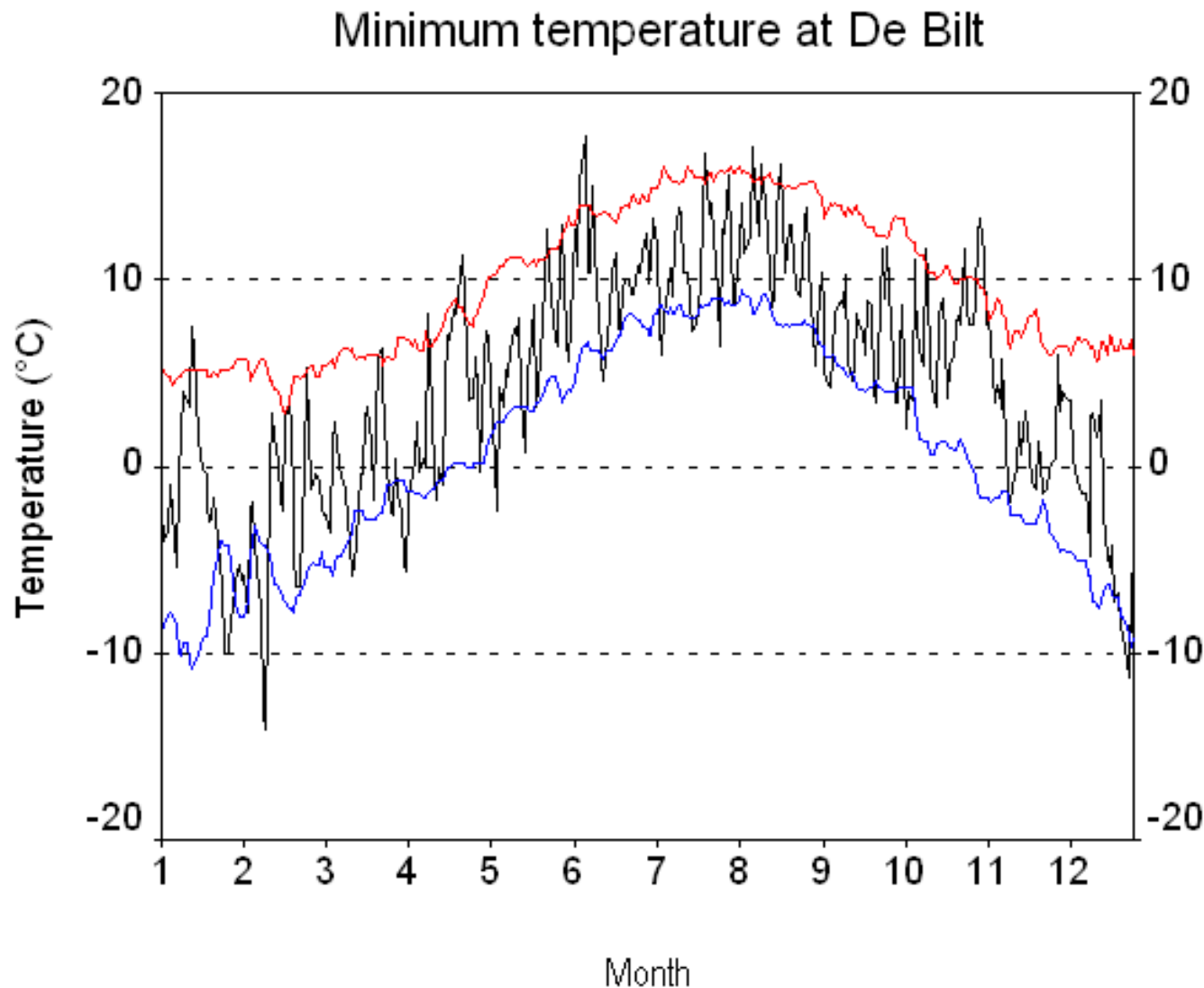
Often not available in obs

=> moderate extremes

# Analysis of extremes

- For analyzing moderate extremes an internationally coordinated set of descriptive indices can be used, which describe frequency, amplitude, persistence
- User-friendly R-based software (RClimDex) for their calculation is available from <http://cccma.seos.uvic.ca/ETCCDI>
- cdo software (<https://code.zmaw.de/projects/cdo>) can also calculate them
- One key approach involves counting the number of days in a season or a year that exceed specific thresholds

# Analysis of extremes

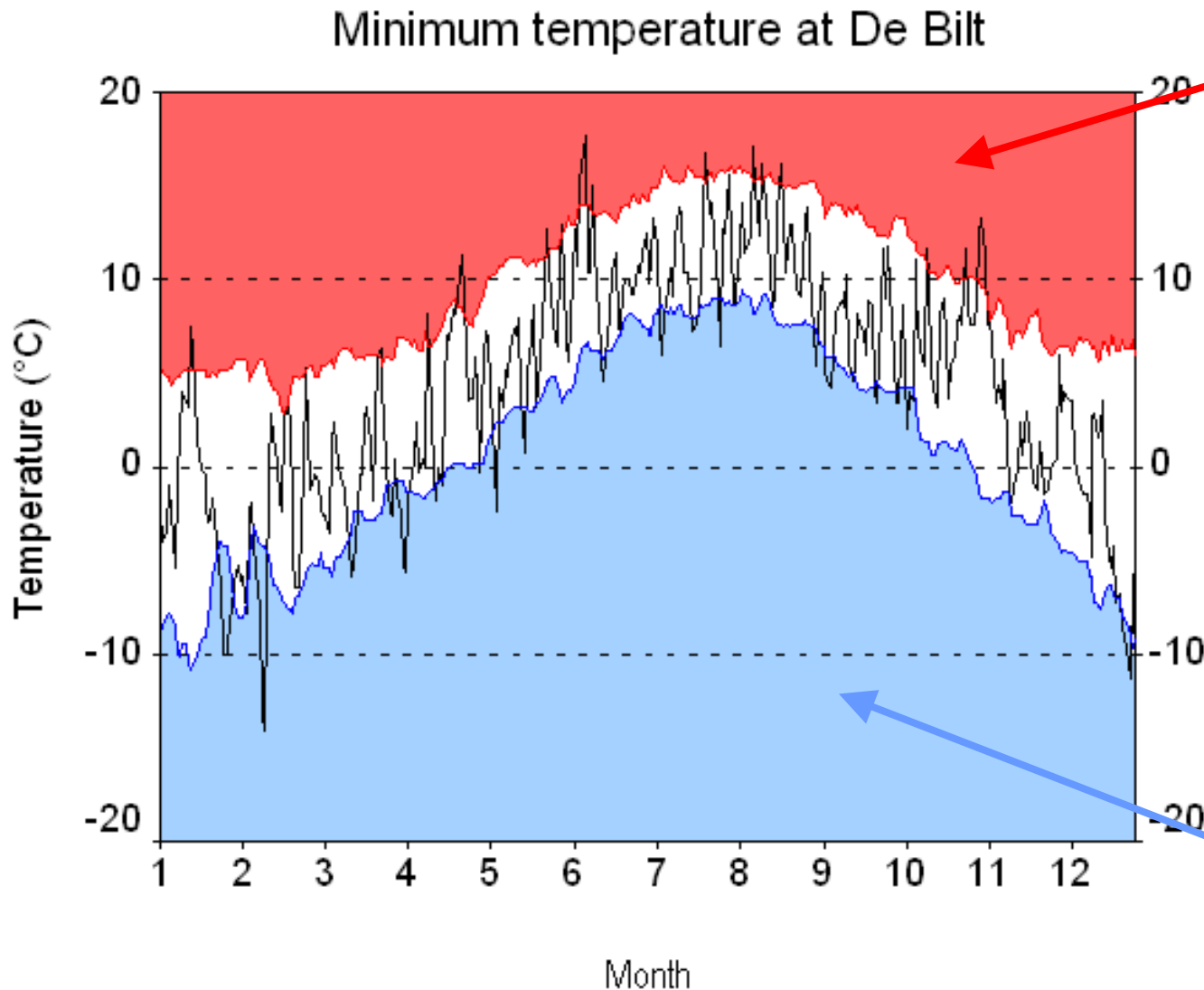


upper 10%-ile  
1961-1990

the year 1996

lower 10%-ile  
1961-1990

# Analysis of extremes



“warm nights”

upper 10%-ile  
1961-1990

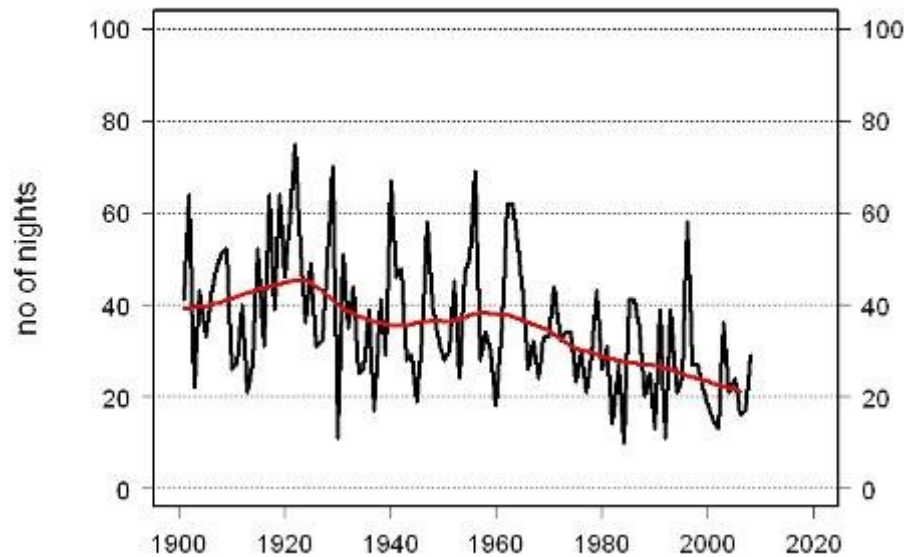
the year 1996

lower 10%-ile  
1961-1990

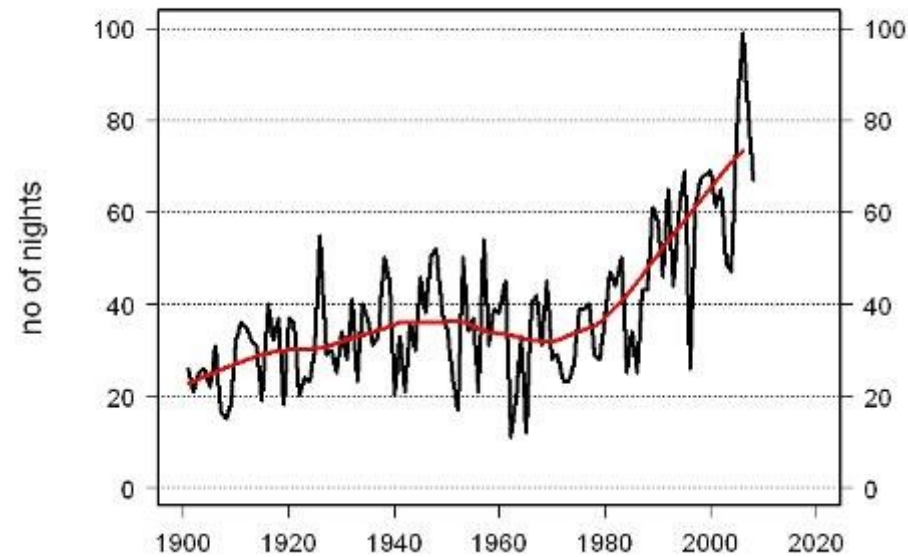
“cold nights”

# Analysis of extremes

c) TN10p, cold nights



d) TN90p, warm nights



De Bilt, the Netherlands

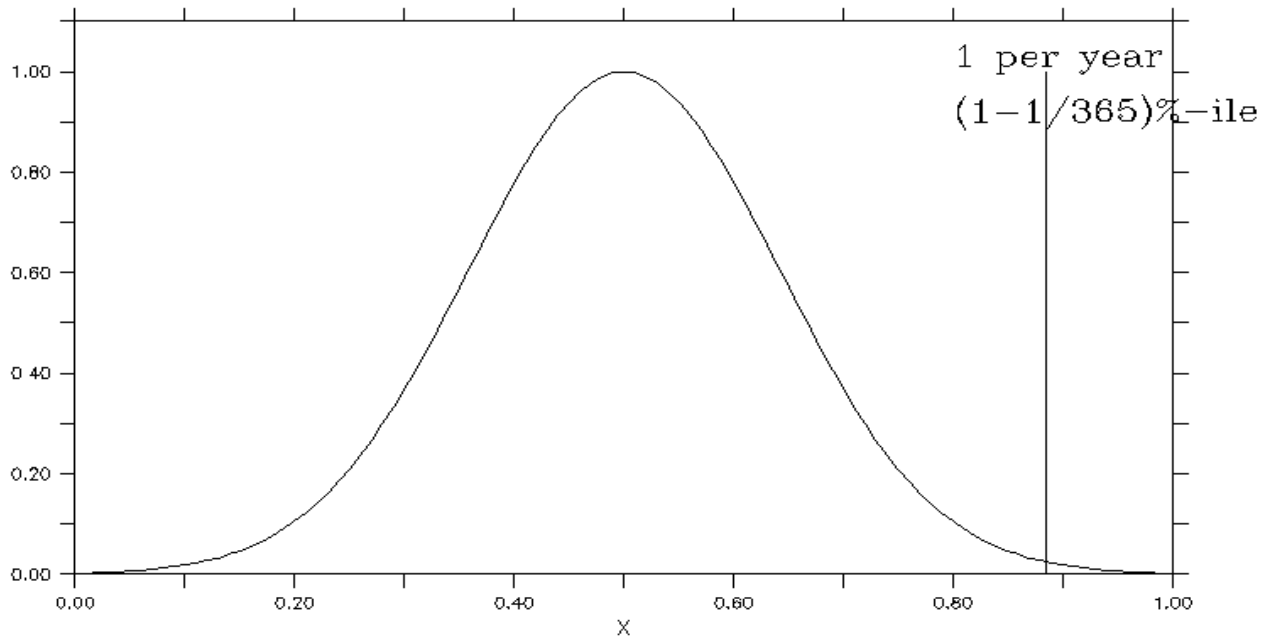


## EVT - 1

Extremes: tail of a distribution

=> few observations

=> tail badly constrained





## EVT - 2

Fortunately, the tails of distributions behave similarly.  
They are described by **Extreme Value Theory**.

Two basic approaches:

1. Block-maxima ( $\Rightarrow$  GEV)
2. Peak-over-Threshold (POT;  $\Rightarrow$  GPD)



## GEV

Under very general conditions the distribution of block-maxima is given by the GEV distribution

$$G(x) = \exp \left\{ - \left[ 1 + \xi \left( \frac{x - \mu}{\sigma} \right) \right]^{-1/\xi} \right\}$$

$$1 + \xi \left( \frac{x - \mu}{\sigma} \right) > 0$$

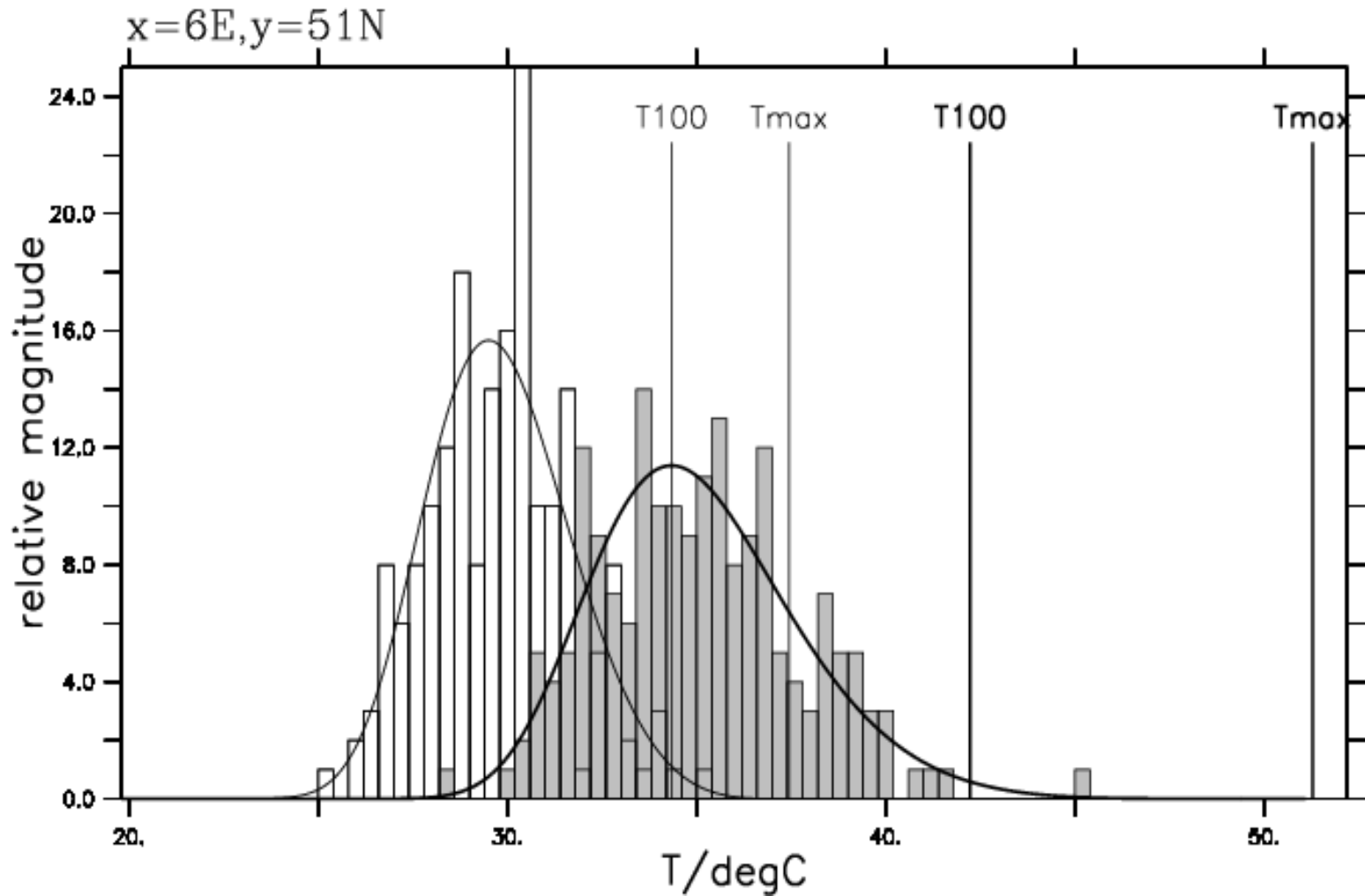
$\mu$ : location

$\sigma$ : scale

$\xi$ : shape



# Example: Temperature in the Netherlands





## Visualization: Gumbel plot

Plot as function of Gumbel variate

$$x = -\ln(-\ln(G(y)))$$

$\xi$  = curvature; straight line for  $\xi = 0$  (Gumbel distribution)

$\sigma$  = slope

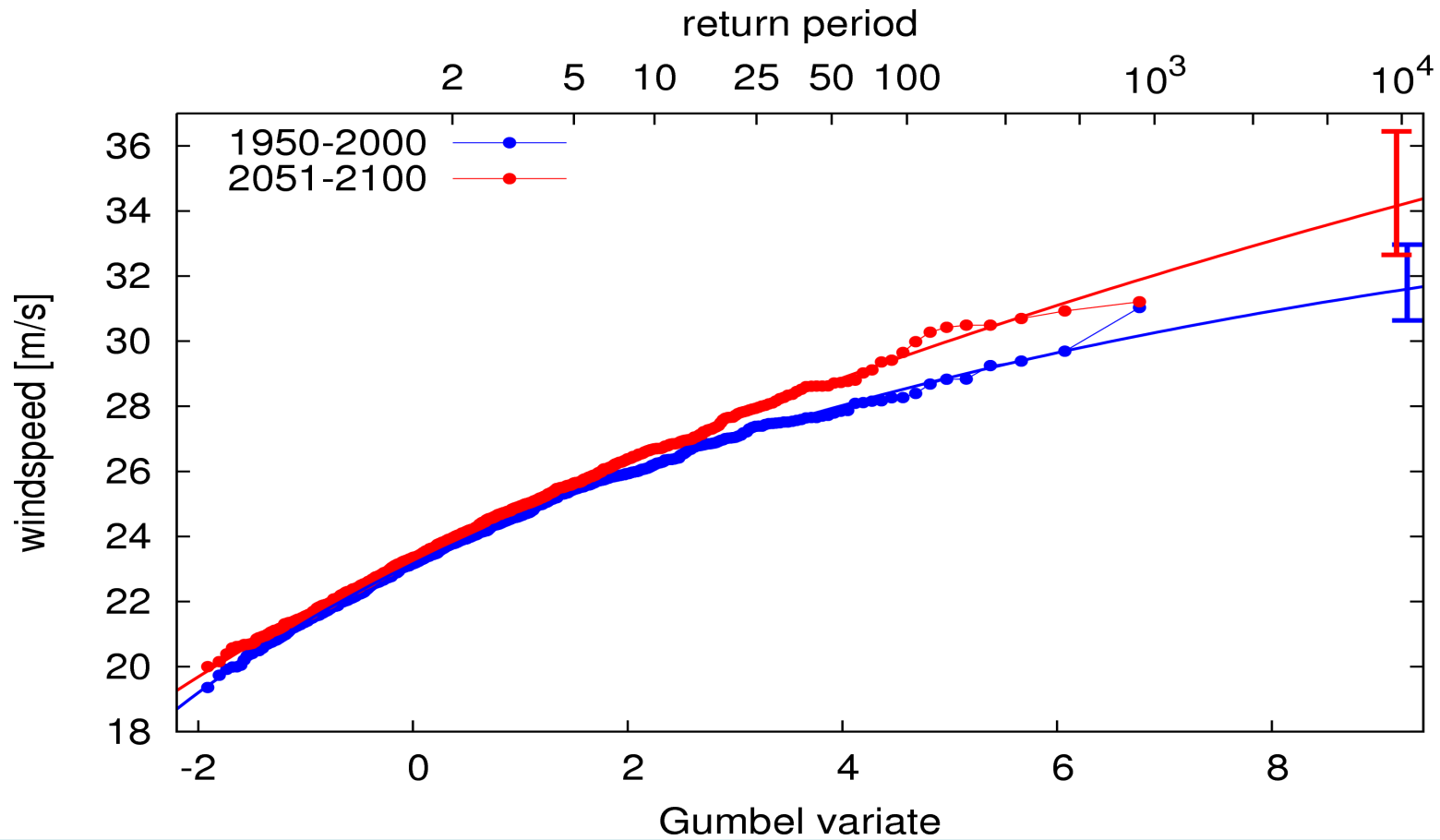
$\mu$  = value at  $x = 0$

One-to-one relation with **return time** (average time between events)



# Example: wind in North Sea

(1.8E;55N)





## POT

Exceedences ( $x > u$ ) follow Poisson process (i.e., intervals between them are Poisson-distributed)

=> exceedences follow GPD:

$$F_u(x) = \begin{cases} 1 - (1 - \kappa x/\alpha)^{1/\kappa} & \text{if } \kappa \neq 0 \\ 1 - \exp(-x/\alpha) & \text{if } \kappa = 0, \end{cases}$$

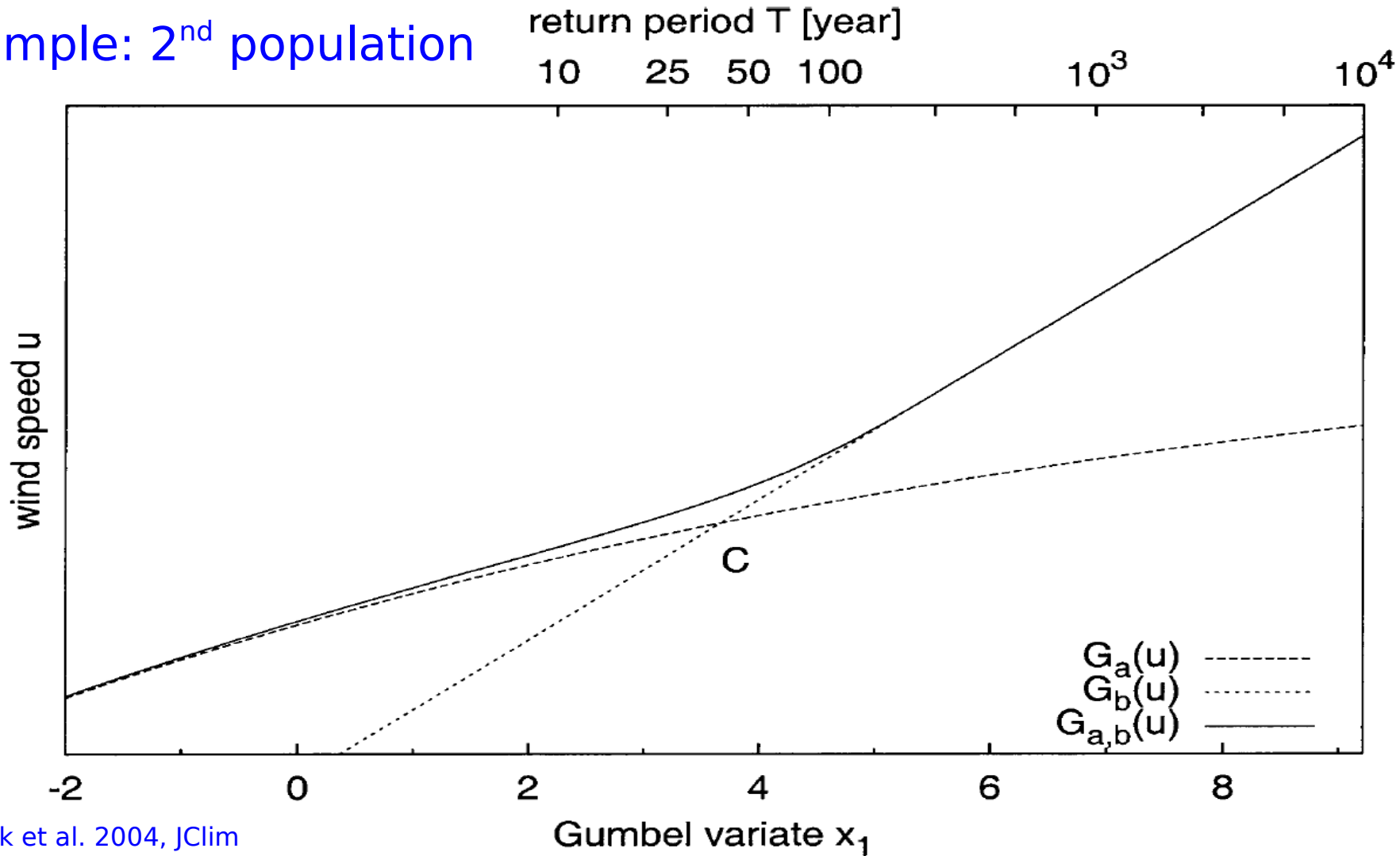


## Considerations

- Distribution => confidence interval
- Choice of block length (threshold)
  - Independent events (=> declustering)
  - Small => more data => greater confidence
  - Large => further out in tail => conditions better satisfied
- Tail must be determined by **one type of process**
  - You have to be far enough in the tail
  - Increasing block length (GEV) or threshold (GPD) should not change result
  - 2<sup>nd</sup> population (large-scale vs. convective precip; cyclone vs. hurricane)
- Increased convergence if fitted to  $x^k$ ,  $k$  = shape of parent distribution



## Example: 2<sup>nd</sup> population



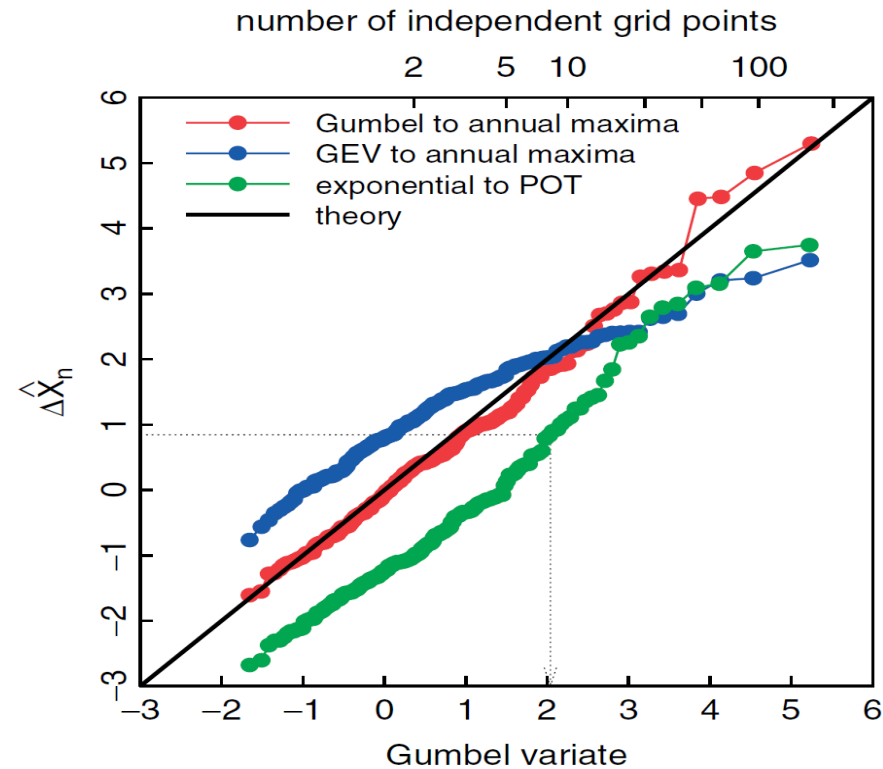
v/d Brink et al. 2004, JCLim



## Henk's method

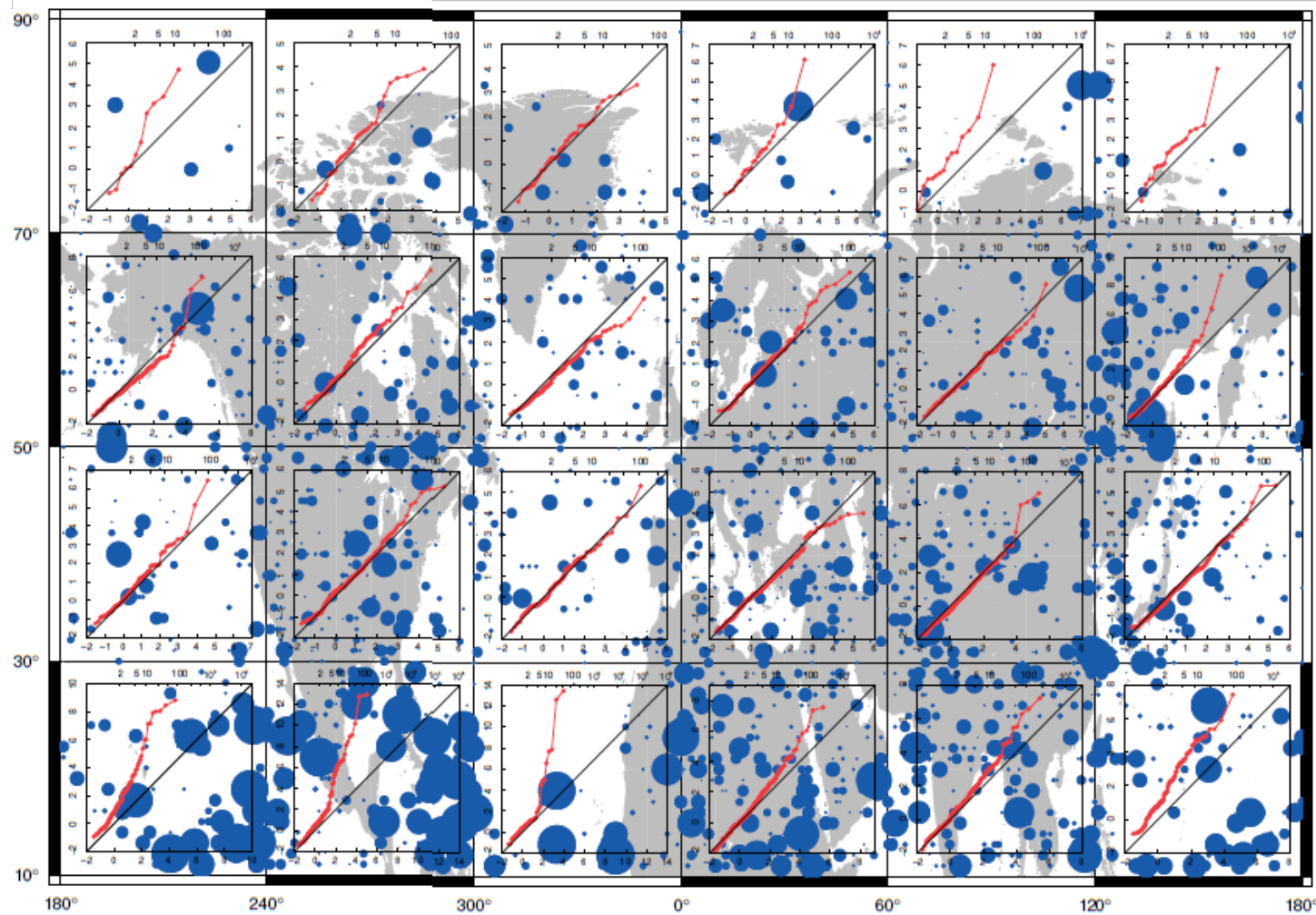
Deviations of the highest event from fit are Gumble distributed.  
Examining a lot of fits, the appropriateness of the chosen distribution can be assessed.

Extreme wave heights (30-70°N) fitted to three different distributions. Deviations of highest events should be Gumble-distributed.  
=> Gumble performs best.





Distributions of highest deviations of ERA-40 winds fitted to a Gumbel distribution. In the tropics a 2<sup>nd</sup> population is visible.



v/d Brink, Können, 2009

# Analysis of extremes

- Among others, a user-friendly R-based toolkit (extRemes) is available from

<http://www.assessment.ucar.edu/toolkit>

(Stephenson and Gilleland, 2006;  
Gilleland and Katz, 2005)



# Example: waterlevels Dutch coast

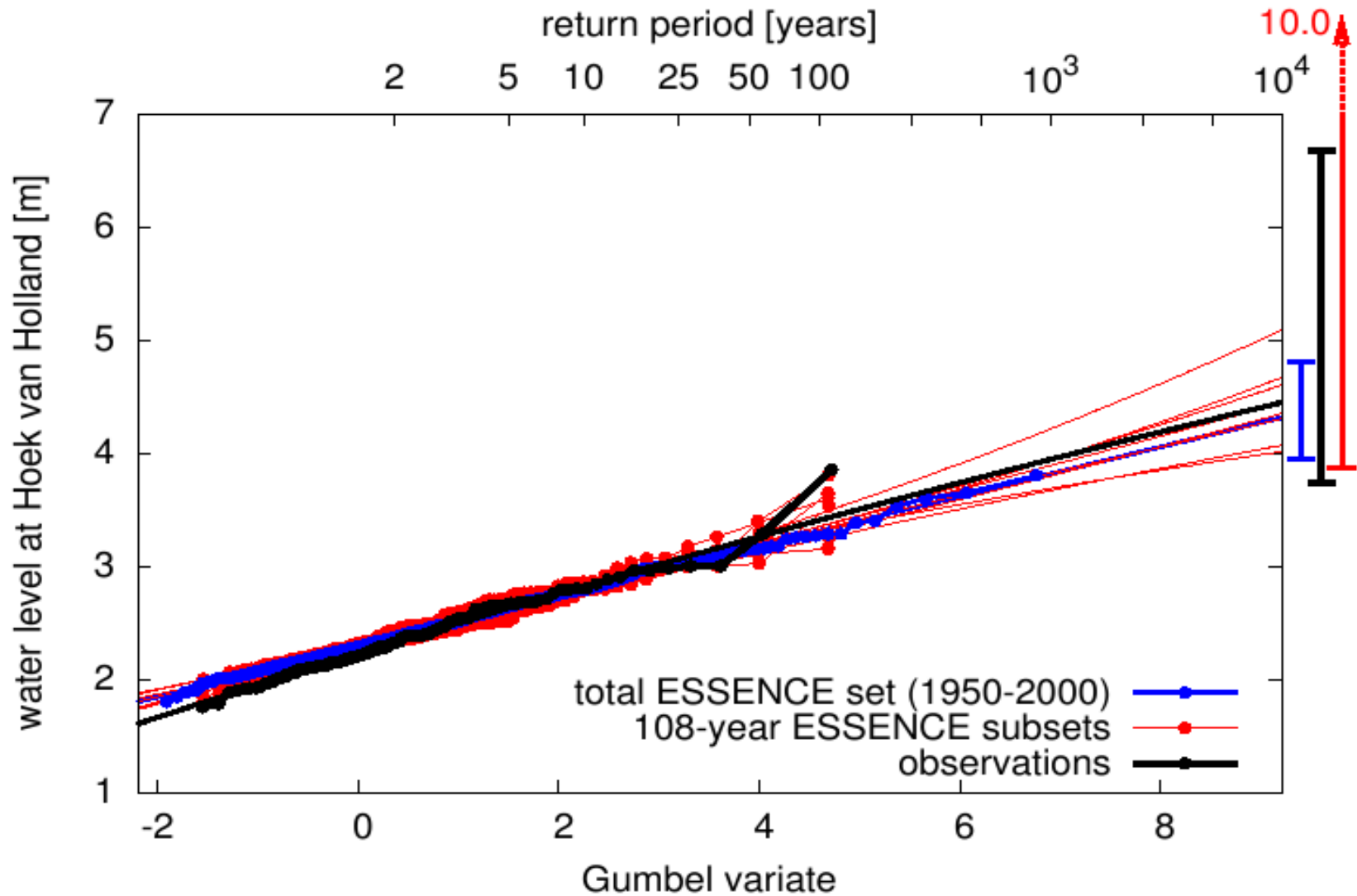
## Essence

ECHAM5/MPI-OM  
17-member ensemble  
1950-2100, SRES A1b

## WAQUA

storm surge model  
Northwest European shelf  
8 km x 8 km  
output every 10 minutes

# Uncertainty present-day water levels



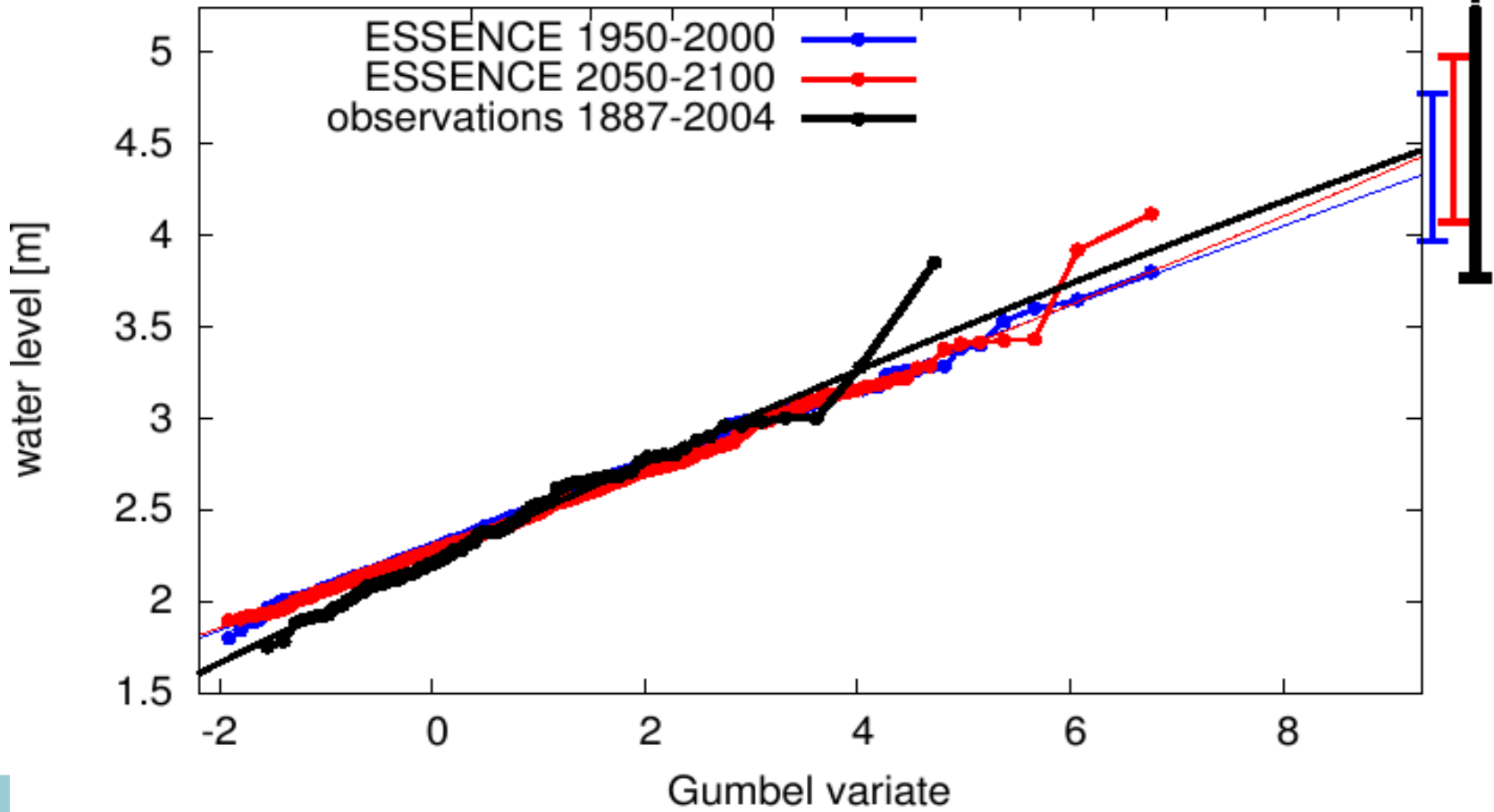
# Future water levels

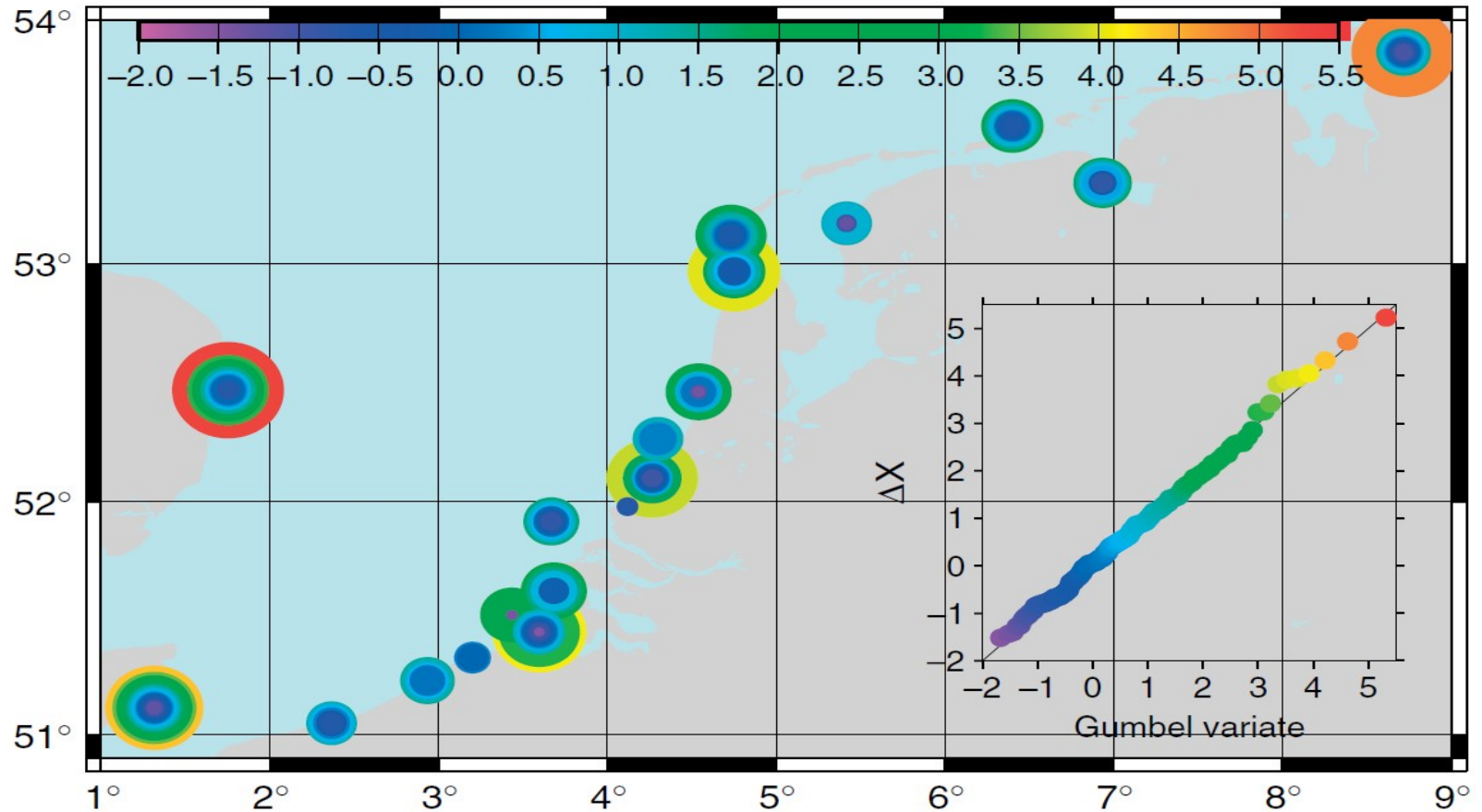


Hoek van Holland

return period

2 5 10 25 50 100  $10^3$   $10^4$





Deviations from a Gumbel-fit (GEV with shape nearly 0): same model can be used for all points

v/d Brink, Können, 2009



# Research Questions

Co-variates, especially time

Make parameters ( $\mu$ ,  $\sigma$ ) time dependent (linear, El Niño)

Attribution

Min et al. 11: change over time; fingerprint method

Poll et al. 11: one specific event; large ensemble

Physical modelling of extremes:

Under what conditions do extremes occur?

Joint probabilities

e.g., heavy rain + surge at same time

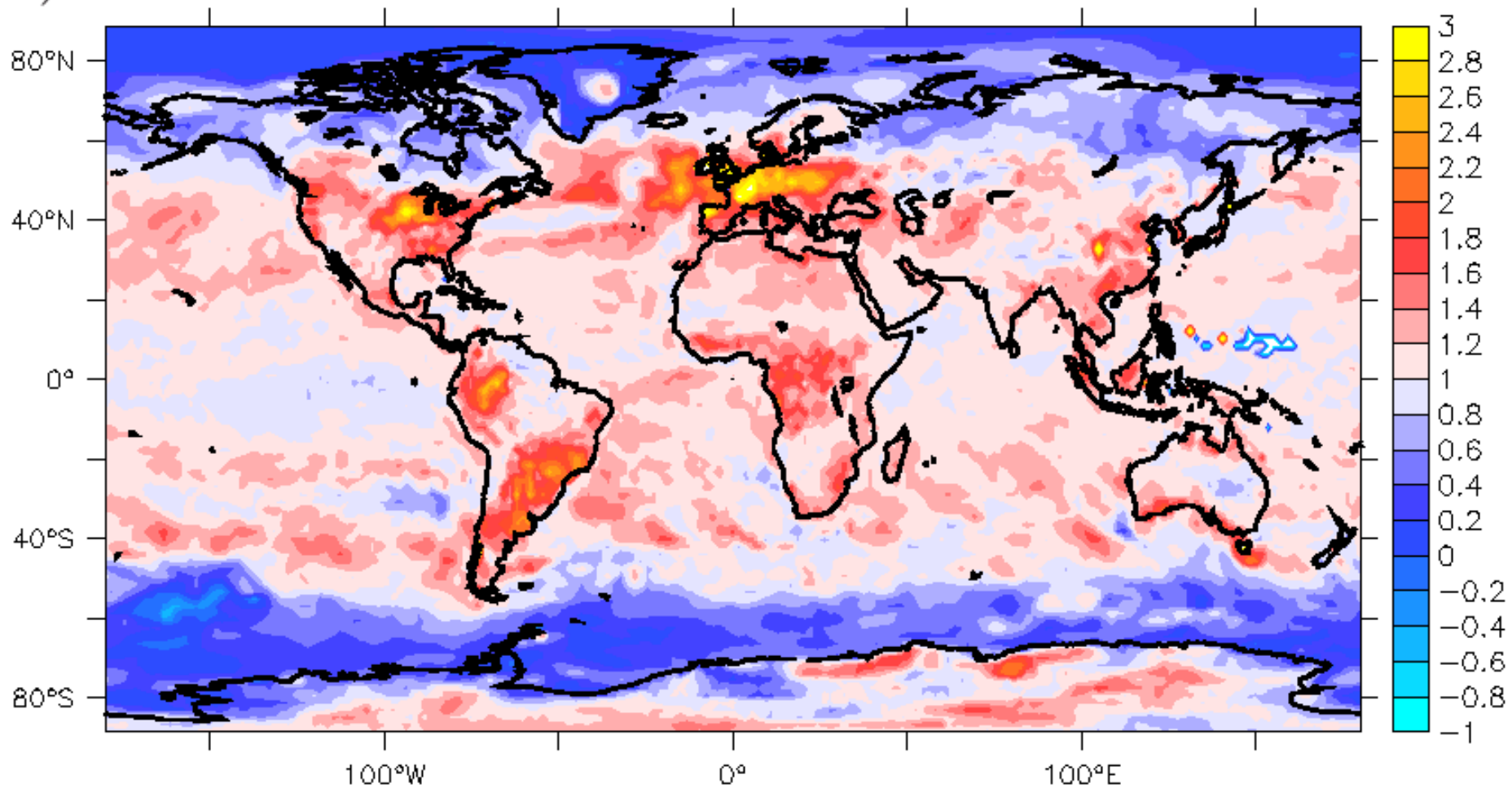
Changes of extremes

shift ( $\mu$ ) or change of shape ( $\sigma$  and/or  $\xi$ )?



a)  $\Delta T_{100}$

$\Delta T_{100} / \Delta T_{\text{mean}}$





## Conclusions

- Extremes are important (vulnerability)
- Rare events => small numbers
- Moderate or soft extremes ( $\sim$  once per year)
  - Simple climate indices
  - Easy to determine (just count)
- Extreme extremes ( $p < \sim 0.1/y$ )
  - EVT, well established
  - extrapolation possible (long return times)
  - Confidence intervals
  - Time dependence



THE END !!!